

Name _____

Date _____

2.7 Prove Angle Pair Relationships

Theorem 2.3--All right angles are congruent

Theorem 2.4-The Congruent Supplements Theorem--

Theorem 2.5-The Congruent Complements Theorem--

Prove Theorem 2.4Given: $\angle 1$ and $\angle 2$ are supplementary $\angle 3$ and $\angle 2$ are supplementaryProve: $\angle 1 \cong \angle 3$

Statements

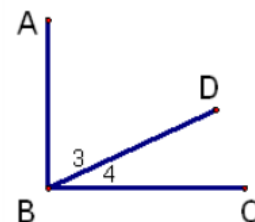
Reasons

Postulate 12—The Linear Pair Postulate--

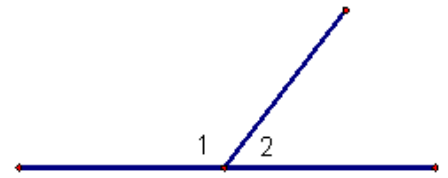
The Complement Theorem—If the noncommon sides of 2 adjacent angles form a right angle, then the angles are complementary angles. (not in book)**Theorem 2.6**—Vertical angles are congruent**How they are used:**Given: $\overline{AB} \perp \overline{BC}$

1. $\angle ABC$ is a right angle
2. $\angle 3$ and $\angle 4$ are complementary

1. Def of \perp lines
2. The Complement Thm.



Given: picture



1. $\angle 1$ and $\angle 2$ are a linear pair.
2. $\angle 1$ and $\angle 2$ are supplementary
3. $m\angle 1 + m\angle 2 = 180$

1. Definition of a linear pair
2. The Linear Pair Postulate
3. Def. of supplementary

Given: $\angle 1 \cong \angle 3$

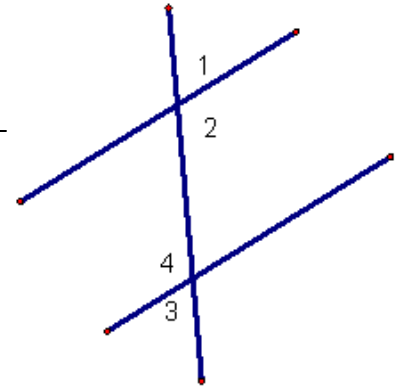
Prove: $\angle 2 \cong \angle 4$

Statements

Reasons

1. $\angle 1 \cong \angle 3$

1. Given



Given: $\angle 1$ and $\angle 2$ are supplementary

Reason: Definition of supplementary angles

Conclusion: $m\angle 1 + m\angle 2 = 180$

Given: $\angle 1$ and $\angle 2$ are complementary

Reason: Definition of complementary angles

Conclusion: $m\angle 1 + m\angle 2 = 90$

Given: $\angle 1$ is a right angle

Reason: Definition of right angles

Conclusion: $m\angle 1 = 90$

Given: $\overline{AB} \perp \overline{BC}$

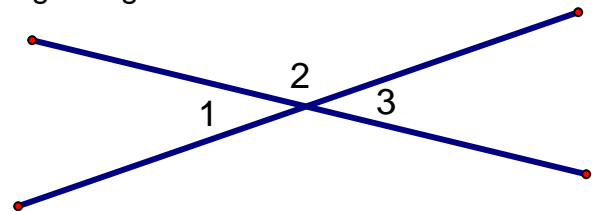
Reason: Definition of perpendicular lines

Conclusion: $\angle ABC$ is a right angle

Proof of theorem 2.6:

Given: picture

Prove: $\angle 1 \cong \angle 3$

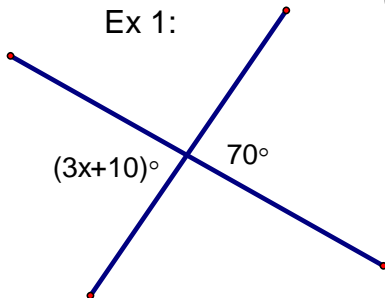


Statements

Reasons

Solve for x and/or y.

Ex 1:



Ex 2:

